# Distributed Computing Column 62 Decidability in Parameterized Verification

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This column consists of an article by Roderick Bloem, Swen Jacobs, Ayrat, Khalimov, Igor Konnov, Sasha Rubin, Helmut Veith, and Josef Widder on automated verification of distributed algorithms. One of the challenges in this area is how to have the number of processors be a parameter, instead of a fixed constant. The authors recently completed a book for the Morgan & Claypool Distributed Computing Synthesis Lectures series on the subject of the decidability of parameterized verification and I thought the readers of this column might enjoy a preview of the book providing a taste of the questions studied in parameterized model checking.

On a very sad note, Helmut passed away unexpectedly during the preparation of this article. He had been working on furthering connections between the formal verification and distributed computing communities, among other projects, and will be greatly missed.

Many thanks to Roderick, Swen, Ayrat, Igor, Sasha, Helmut, and Josef for their contributions!

**Call for contributions:** I welcome suggestions for material to include in this column, including news, reviews, open problems, tutorials and surveys, either exposing the community to new and interesting topics, or providing new insight on well-studied topics by organizing them in new ways.

# Decidability in Parameterized Verification<sup>1</sup>

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<sup>&</sup>lt;sup>1</sup>We dedicate this article to the memory of Helmut Veith, who passed away tragically while this manuscript was being prepared. His curiosity and energy ignited our joint long-term effort in parameterized verification.

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#### Abstract

Parameterized model checking is an active research field that considers automated verification of distributed or concurrent systems, for all numbers of participating processes. In our recent book [11] we surveyed literature on decidability of parameterized verification. The system models, as well as the proof methods, that are studied in this field are similar to those from distributed computing. For instance, we survey results for token passing systems and ad hoc networks. The proof methods for undecidability include simulation of two-counter machines. For decidability, we survey cut-off results that provide conditions to reduce parameterized verification to model checking of fixed-size systems. We believe that the results are of interest to the readers of the Distributed Computing Column, and in this short note we want to give a taste of parameterized model checking.

### 1 Introduction

Designing concurrent or distributed systems and proving their correctness is both difficult and error-prone. There are, roughly speaking, two streams of research that address these tasks. On the one hand, principles of distributed computing are studied in order to develop mathematical proof methods can be used establish complexity results in distributed computing (lower and upper bounds) [34, 8], and to prove the correctness of distributed algorithms. On the other hand, one investigates computer aided verification methods, such as model checking [14]. Mathematical proofs typically consider parameterized systems, where, e.g., the parameter n determines the number of replicas in a distributed system, and one determines the correctness of a distributed algorithm for all values of n. Historically, model checking considers fixed size and finite state systems only. For instance, one fixes n = 4 and checks the small system for presence of bugs. However, nowadays most research in model checking considers parameterization in one way or another, e.g., parameterized number of processes, or parameterized domain of variables. Consequently, there is a vast literature in this domain.

Our recent book [11] focuses on automatic verification of systems where the number of processes is parameterized, while the local state space of the processes is finite. More precisely, we consider the decidability of parameterized model checking of concurrent systems. The literature in this field considers different computational models and we thus survey results for the most studied models: token passing systems, systems where processes coordinate by pairwise rendezvous or one-to-many synchronization (broadcast), guarded protocols, and finally ad-hoc networks.

In this note, we briefly discuss the features of these computational models and some conclusions we have drawn from surveying the literature. For formal definitions as well as a detailed survey of the results and their proofs we refer to the book. We start with discussing the computational model used in the book in Section 2 and some often-used proof techniques in Section 3, and then describe the different system models that are covered in the book, and summarize their decidability results in Sections 4 to 7.

# 2 Models and Specifications

Finding out whether parameterized model checking is decidable for one's favorite computational model boils down to checking whether the model is captured by the semantics of one of the published computational models. However, computational models are scattered over the literature and use different terminology, and results are based on slightly different assumptions. Hence, it is cumbersome to check whether existing results apply to our favorite models. Our motivation was to provide a one-stop-source for results that eases this task. This required us to provide a definition for concurrent systems that incorporates many of the foundational computational models in the parameterized model checking literature. The models we discuss in Sections 4 to 7 specialize specific features of this general model.

In our framework, a concurrent system, or system instance,  $\overline{P}^G$  is composed of a vector of process templates  $\overline{P} = (P^1, \ldots, P^d)$ , and a graph G, on which copies of the templates are arranged. We consider discrete time, and at each time step either one process acts alone, or some process v initiates an action and some set of processes that are connected to v in G simultaneously synchronize with v. Thus, we consider that processes coordinate instantaneously using synchronization primitives (e.g., rendezvous), and do not consider, e.g., non-blocking communication by message buffers. Most importantly, the process templates we consider have a fixed and finite local state space.

Synchronization primitives can then be defined by restricting the number of processes that can simultaneously synchronize with the initiating process. We do so by a so-called *synchronization* constraint that specifies how many processes should synchronize. For instance, pairwise rendezvous is captured by having the singleton  $\{1\}$  as synchronization constraint, which means that every synchronous transition must be taken by the initiating process and exactly one other process.

Then, a parameterized system is a sequence of system instances formed from a fixed vector of process templates and a sequence of graphs **G**. Typical sequences of graphs are rings of size n, cliques of size n, or stars of size n, where n is the parameter. The nth instance of a parameterized system is the system instance  $\overline{P}^{\mathbf{G}(n)}$ . Parameterized specifications make statements about parameterized systems by quantifying over process indices (i.e., vertices of  $\mathbf{G}(n)$ ), e.g., "every process v of  $\mathbf{G}(n)$  eventually satisfies predicate p". To formalize this, we recall the definitions of several indexed temporal logics in the book. The parameterized model checking problem (PMCP) is to decide whether for all  $n \in \mathbb{N}$  the instance  $\overline{P}^{\mathbf{G}(n)}$  satisfies the specification.

### **3** Proof Techniques

#### 3.1 Undecidability

In this area, undecidability is typically proven by reduction from the non-halting problem of twocounter machines, which is known to be undecidable. In the proof, one then shows how to simulate up to n steps of a two-counter machine in a system composed of n+1 finite-state processes: There is a *controller* process that simulates the internal state of the two-counter machine. The remaining nprocesses collectively encode the counter values in a way that allows for storing values up to n, which is the maximal value that can be written in n steps. The proofs differ in how the controller uses the synchronization primitives to issue commands to increment/decrement counters and test counters for zero.

The prototypical such proof in a token ring is by Emerson and Namjoshi [27] and describes a distributed algorithm that performs this task. This improved the first undecidability results for systems consisting of identical processes arranged in a uni-directional ring with a single multi-valued token by Suzuki [41] who reduces non-halting of Turing machines to parameterized model checking. Undecidability of parameterized model checking then follows from undecidability of the non-halting problem.

#### 3.2 Decidability

One way to prove decidability of parameterized verification for a certain class of concurrent systems is to show that this class can be represented as a well-structured transition system [29]. For such systems Abdulla et al. [2] provided a comprehensive theory.

A quite intuitive approach to parameterized model checking is to check the system for small values of n and assume that if there is a bug in a system with a large number of components, then the bug already appears in the small system. This approach can be formalized as a *cutoff* or decomposition statement [27, 15] that reduces the parameterized model checking problem to a finite collection of classic model checking problems. For specific classes of systems one can show that such cutoffs or decompositions indeed exist, from which decidability of parameterized model checking for such systems follows. To prove that c is a cutoff for a class of systems and specifications in an indexed temporal logic, it suffices to show that a system with exactly c components relates to a system with arbitrarily many components. The details of the specific relation (e.g., simulation or bisimulation) depend on the class of systems and the temporal logic under consideration.

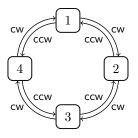
## 4 Token-passing Systems

In a token-passing system (TPS), processes communicate by passing a token in the network. The token may or may not carry a value that can be updated by the process that holds it. In case of a valueless token, the only purpose of the token is to distinguish the process that currently holds it from all the other processes, which allows one for example to implement systems with mutual exclusion properties.

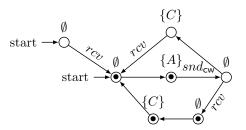
A well-known example system that can be modeled as a TPS with valueless token is *Milner's* scheduler [36]. The scheduler is composed of an arbitrary number of components, each of which is responsible for activating some (unspecified) task and receives confirmation when its task has been executed. Scheduling should ensure that the tasks are activated in a round-robin scheme, and that every task has terminated before being activated again. As noted by Emerson and Namjoshi [27], this can naturally be modeled in a token ring. That is, processes are arranged in a ring, and one process starts with the token. A process that has the token will activate its task, and then send the token to the next process. After starting the task, it will wait for both the return of the token and a confirmation that the task has terminated. Only after both of these events, the process will activate its task again. Thus, communication by a single valueless token is sufficient to guarantee the global properties required by the Milner scheduler. The graph and process template for Milner's scheduler in a token ring are depicted in Figure 1.

For other classes of systems, the parameterized verification literature usually considers a single fixed graph structure, like cliques for systems with broadcast communication or guarded protocols. In contrast, TPSs have been analyzed on a variety of graphs that can be much more complex. In particular, this includes graphs where connections may be labeled with directions, and processes can choose in which direction they want to send the token. Finally, another orthogonal extension of the model considers systems with multiple tokens.

**Results.** Most of the decidability results in the literature are for TPSs with a single valueless token [27, 15, 5], and where token passing satisfies some notion of fairness. However, even in systems with such a restricted communication primitive, parameterized model checking is undecidable if we



(a) A bi-directional ring with 4 nodes. Edges are labeled with directions cw (clockwise) or ccw (counter-clockwise). Processes can send the token in a direction by using actions  $snd_{ccw}$  or  $snd_{ccw}$ , respectively.



(b) Process template for Milner's scheduler. States with token are depicted with a dot inside. State labels are depicted above states. Label A stands for activation of the task, C for completion of the task.

Figure 1: Milner's scheduler in a token ring.

consider arbitrarily complex graphs and specifications in a branching-time logic. Undecidability proofs show that such systems can simulate two-counter machines, and deciding the PMCP would decide the non-halting problem of these machines [15, 5]. To obtain decidability results, the literature considers restrictions on the graph structure, as well as on the number of index and path quantifiers in the specification.

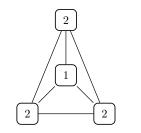
For rings, Emerson and Namjoshi [27] have identified concrete cutoffs between 2 and 5, depending on the specification, but independent of the process template. Cutoffs for rings and some other classes of graphs can be found by manually constructing a bi-directional simulation as mentioned in Section 3.2 [27, 5]. In TPSs with possibly complex graphs, this simulation needs to take into account whether processes mentioned in the specification are direct neighbors or not, and consider all possible cases of neighborship relations if the specification quantifies over multiple processes. For certain classes of graphs that can be constructively specified, cutoffs can also be computed automatically [6].

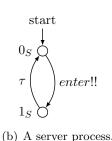
If tokens can carry values, decidability is lost even in uni-directional rings [41]. Similarly, if processes can distinguish directions in the graph, we get undecidability in bi-directional rings [5]. To recover decidability, additional restrictions on graphs, processes, or specifications are necessary.

# 5 Broadcast and Asynchronous/Pairwise-Rendezvous

The broadcast communication primitive is an abstraction of, e.g., ethernet-like broadcast, GSM's cell-broadcast, communication in Prasad's Calculus of Broadcasting Processes (CBP) [39], or the notifyAll method in Concurrent Java [18]. To use the broadcast communication primitive, an initiator process sends a message and every process that is able to receive the message (if any) immediately and simultaneously does so. Figure 2 illustrates a client-server system with three clients. If the server broadcasts the message enter by firing the transition from state  $0_S$  to  $1_S$ , then, simultaneously, every client that is in state  $0_C$  transitions to  $1_C$ .

Two other related primitives are asynchronous-rendezvous in which exactly one process that is able to receive the message does so (if any), and pairwise-rendezvous which is like asynchronousrendezvous except that sending is blocked if there is no process that is able to receive. Asynchronousrendezvous is an abstraction of, e.g., the **not**ify method in Concurrent Java [18], and pairwiserendezvous is like synchronized communication in Milner's Calculus of Communicating Systems





start  $0_C \longrightarrow \tau$   $\tau$  enter??  $1_C \bigcirc$ (c) A client process.

(a) A clique graph with three clients and one server.

Figure 2: A Client/Server system.

(CCS) and Hoare's Communicating Sequential Processes (CSP).

Broadcast can express many others primitives including asynchronous- and pairwise-rendezvous, token-passing (Section 4) and disjunctive guards (Section 6) [7].

**Results.** We assume the communication graph is a clique (other graphs are assumed in Sections 4 and 7). Parameterized model checking of broadcast systems is undecidable for liveness properties (e.g., some state from a given set is seen infinitely often), and decidable for safety properties (e.g., no state from a given set is ever visited). The proof of undecidability uses the basic encoding of two counter machines outlined above. The interesting part of the simulation is testing a counter for zero, and uses a trick in which the controller broadcasts a guess of whether the counter is zero or not, thus potentially introducing errors to the simulation, which can be compensated for, however. Decidability of safety properties follows from the fact that broadcast systems are well-structured transition systems [2]. The case of asynchronous-rendezvous is similar.

On the other hand, for pairwise-rendezvous, both liveness and safety specifications are decidable. The proof of this fact shows that such systems can be expressed as Petri Nets or Vector Addition Systems [28]. The main idea is to use a counter-representation that captures, for each configuration, the number of processes in each state. Thus configurations are represented as vectors of natural numbers, and a rendezvous between two processes corresponds to adding a fixed vector to a configuration.

All the results above are for linear-temporal specifications. Branching-temporal specifications are undecidable already for pairwise rendezvous [6].

### 6 Guarded Protocols

The key feature of guarded protocols is that every process can query the local states of the other processes in an anonymous way. For instance, a process j evaluates the disjunctive guard  $[\exists \text{ other } i] A_i \lor B_i$  to true, whenever a global state contains a process i (other than j) that is either in local state A, or B. Likewise, a process j evaluates the conjunctive guard  $[\forall \text{ other } i] A_i \lor B_i$  to true, whenever all processes different from j are either in A, or in B. While the seminal paper by Emerson and Namjoshi [26] introduced guarded protocols for synchronous systems, the follow-up papers by Emerson and Kahlon [23, 24, 25] considered asynchronous guarded protocols.

Guarded protocols have been used to model cache-coherence protocols (e.g., [24]). A more classical example is a *multiple* readers and *single* writer protocol shown in Figure 3. The read-

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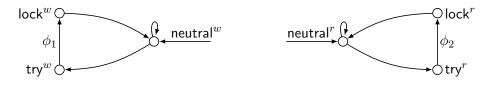


Figure 3: A readers/writer protocol.

ers start in the state neutral<sup>r</sup>, and the writers start in the state neutral<sup>w</sup>. A writer's transition from the trying state  $\operatorname{try}^w$  to the locking state  $\operatorname{lock}^w$  is guarded with the guard  $\phi_1 \equiv [\forall \operatorname{other} j] \operatorname{neutral}_j^r \lor \operatorname{neutral}_j^w \lor \operatorname{try}_j^r \lor \operatorname{try}_j^w$ , which forbids this writer to make a transition, if some readers or writers are in the locking state. A reader makes a transition from the trying state  $\operatorname{try}^r$ to the locking state  $\operatorname{lock}^r$ , only if all writers are in the neutral state, that is, the guard  $\phi_2$  is  $[\forall \operatorname{other} j] \operatorname{neutral}_i^r \lor \operatorname{neutral}_i^w \lor \operatorname{try}_i^r \lor \operatorname{lock}_i^r$ .

**Results.** Unfortunately, parameterized model checking of boolean guarded protocols — that is, protocols that use both disjunctive and conjunctive guards — is undecidable [26]. As usual, undecidability is shown by simulating two-counter machines. Thus, the research has been focused on verification of systems that have only one kind of guards [23, 24, 25].

As shown by Emerson and Kahlon [23], each system composed of n processes having Q local states and using only disjunctive guards has a cutoff of size |Q| + 2. Hence, to check a temporal property for all system sizes, it is sufficient to check the property for systems of size up to |Q|+2. A cutoff of size 2|Q|+1 was also found [23] for systems with conjunctive guards having the following restrictions: every process can remain indefinitely long in the initial state, and no guard evaluates to false due to a process staying in the initial state.

Further, Emerson and Kahlon showed that systems with disjunctive guards can be simulated by systems with rendezvous communication [25]. Hence, one achieves decidability of PMCP for the systems that use both disjunctive guards and rendezvous communication.

In most cases, extending guarded protocols with broadcast leads to undecidability [25]. The only known decidability result is for regular action-based properties [25], that is, the properties that can be described with a finite automaton recognizing words over the alphabet of action labels.

Finally, Emerson and Kahlon developed special techniques for the restricted versions of guarded protocols that model cache coherence protocols [24].

# 7 Ad Hoc Networks

In ad hoc networks, processes communicate using "local" broadcasts: such messages are visible only to processes in the communication range of the sender. Ad hoc networks can be captured by broadcast systems (Section 5) if we model the communication ranges using the system graph: two nodes are connected only if in the ad hoc network the two processes can hear each other.

Figure 4 illustrates a Request-Acknowledgment-OK protocol to be run by processes of an ad hoc network, and a possible state after executing the protocol. The intention of the protocol is to "create" pairs of connected processes in states  $l_3$  and  $s_3$  that are isolated from others by processes in state *err*.

In contrast to other systems considered in our survey, the literature on ad hoc networks [19, 20, 21, 1] does not study the PMCP for a general class of specifications, but rather three specific

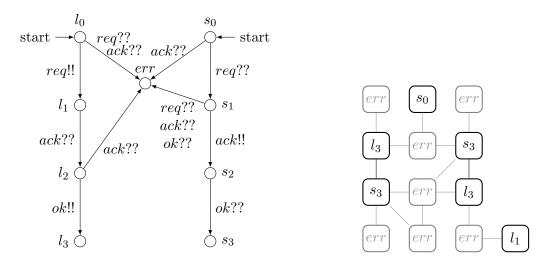


Figure 4: On the left: Request-Acknowledgment-OK protocol for ad hoc networks [19]: initial states are  $\{s_0, l_0\}$ , a!! means "broadcast message a", and a?? means "receive message a" (for  $a \in \{req, ack, ok\}$ ). On the right: example state after running the protocol.

problems called COVER, REPEAT, and TARGET. COVER asks, given a process description and a process control state, whether the control state can be reached in a network of some size. Similarly, REPEAT asks if the state can be reached infinitely often, and TARGET asks if all processes can simultaneously reach the state. The first two problems can be expressed as a PMCP using indexed temporal logic with index quantifiers in prenex form, but the last one requires a non-prenex fragment.

The literature also differentiates the results for different classes of graphs. We survey results for five classes of undirected graphs, inspired by those found in practice, including cliques, wheels, stars, processes arranged in clusters, and unrestricted graphs. We also survey results [1] for directed graphs. Such graphs can model discrepancies in the send and receive transmission ranges of processes.

Finally, the literature distinguishes ad hoc networks with and without failures. The failure model is: any broadcast message can be lost non-deterministically for some of the recipients. A related model is that of mobile networks, in which the network graph can non-deterministically change during the execution. Delzanno et al.[21] showed that the models of lossy and mobile networks are equivalent, so we focus on the former only.

**Results.** Roughly, COVER for ad hoc networks without failures is undecidable on graphs that can have simple paths of unbounded length, except cliques (e.g., wheel-like graphs) [19]. The undecidability proof uses the ability of the network to simulate a given two-counter machine, as follows. First, the network runs a special protocol that shuts down all processes except one leader connected to two lists of processes. Then, the leader simulates the control of the two-counter machine using the two lists to store the values of the counters. In this construction, to be able to store the unbounded values of the counters, the two lists should be of unbounded length (unbounded in the parameterized system).

COVER is decidable on graphs in which all simple paths have bounded length [19, 20]. The

decidability proofs go via the machinery of well-structured transitions systems. Intuitively, the proofs use the insight that behaviours of an infinite family of networks have a finite basis, and the basis can be found using a saturation algorithm. Note that REPEAT and TARGET are undecidable on all graph classes we survey, if considered on ad hoc networks without failures [19].

All three problems become decidable for the case of lossy ad hoc networks [21]. The hostile failure model makes it impossible to simulate a two-counter machine, and the decidability proofs go via reduction to Petri nets (a certain kind of well-structured transition systems).

## 8 Conclusions

We believe that parameterized model checking and distributed computing could both benefit from studying parameterized verification in the context of state-of-the-art computation models for distributed algorithms. To initiate a dialog between the concerned communities, in this short note we wanted to give the distributed computing community a taste of the questions studied in parameterized model checking. More details can be found in our recent book [11].

While our initial goal in writing the book was to give a comprehensive survey on parameterized model checking, we quickly learned that the field is too lively for that. Consequently, we limited ourselves to decidability issues in concurrent systems of identical finite state processes. Indeed, our survey is just one in the area of parameterized model checking. Most recently, Delzanno [17] surveyed broadcast protocols. Before that Zuck and Pnueli [43] surveyed abstraction techniques. Regular model checking was surveyed by Abdulla [4], well-structured transition systems were surveyed by Finkel and Schnoebelen [29], and decidability in Petri nets was surveyed by Esparza [28].

Several parameterized model checking techniques have been implemented in tools such as BOOM [10], BYMC [12], T(O)RMC [33], TLV [38] and JTLV [37], Undip [3], MCMT [30], CHEAPS [32], MCMAS-P [35], and Cubicle [16]. Furthermore, there is a number of tools that implement more general forms of infinite-state model checking, in particular with support for integer-valued variables. With a suitable encoding, these tools can be used for parameterized model checking. Examples of such tools are ALV [42], BRAIN [40], FAST [9], MONA [22], and NUXMV [13]. Finally, the tool PARTY [31] uses decidability results surveyed in our book to synthesize parameterized systems from specifications.

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